On the Frequency Dependence of the Bias Temperature Instability


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Abstract—An accurate understanding of the duty-factor and frequency dependence of the bias temperature instability (BTI) is essential since it can transfer to significant lifetime benefits. Contradictory reports regarding the frequency dependence have been published in literature, with particularly older studies and those interpreted in the framework of the reaction-diffusion model claiming BTI to be frequency-independent. Newer studies, on the other hand, clearly show a frequency-dependent component of BTI. Here we discuss this frequency dependence using the recently suggested capture/emission time map model, which explains BTI as a collection of a large number of independent first-order reactions of defects with two states. While this model can explain most features observed in DC and low-frequency AC stress experiments, it does not fully capture the experimentally observed frequency and duty-factor dependence. However, when a more accurate defect model is considered, which describes charging of the defect via an intermediate state, good accuracy with experimental data is obtained.

I. INTRODUCTION

Compared to a conventional DC stress, AC stress patterns can significantly reduce the accumulated degradation [1–4]. In order to properly predict the potentially enormous lifetime benefits, this feature has to be fully understood. For example, assuming that the degradation follows an effective power-law with exponent 0.1, a reduction of the degradation due to AC effects by 10, 30, or 50% results in a lifetime improvement by a factor of 3, 35, and 1000, respectively.

While all studies report a duty-factor dependence following the ubiquitous step-shaped curve [1, 2, 5–8], the frequency dependence of BTI appears to be controversial: particularly older studies using slow measurements report frequency independence of BTI [1, 9, 10], while more recent studies have revealed a frequency dependent contribution [3, 11–20]. We study the duty-factor and frequency dependence in the light of the recently proposed capture/emission time (CET) map model [7, 21–23] and demonstrate that the recoverable component of BTI can only to the first-order be captured by a two-state defect model. By using a three-state defect model, consistent with detailed studies on the microscopic defect properties [24, 25], the experimentally observed frequency dependence can be reproduced for a wide range of technologies.

II. CAPTURE/EMISSION TIME MAP MODEL FOR BTI

It has recently been shown that both static as well as dynamic BTI can be described by an ensemble of first-order defect reactions with a wide distribution of capture and emission times [21]. This model has been validated for various combinations of stress and recovery times for NBTI on SiON/pMOSFETs [7] and PBTI on high-k nMOSFETs [7, 22] both under static and dynamic conditions. The wide distribution of time constants is visualized in the CET map, which can be directly extracted from experimental \( \Delta V_{th}(t_s, t_r) \) recovery curves for various stress and recovery times \((t_s, t_r)\) as [21]

\[
g(\tau_c, \tau_e) = -\frac{\partial^2 \Delta V_{th}(\tau_c, \tau_e)}{\partial \tau_c \partial \tau_e}. \tag{1}
\]

The CET map \( g(\tau_c, \tau_e) \) can be visualized as a function of the effective capture and emission times \( \tau_c \) and \( \tau_e \). In a way, the CET map \( g(\tau_c, \tau_e) \) contains the spectral information of the \( \Delta V_{th}(t_s, t_r) \) curves, very much like in the Fourier transform theory [7].

The beauty of this empirical but physics-based concept is that the effective CET maps are directly accessible to experiment via eq. (1), thereby clearly demonstrating the wide distribution and weak correlation of the effective capture and emission times. This allows for a convenient evaluation of theoretical models which then have to be able to explain the experimentally observed distribution in \( g(\tau_c, \tau_e) \).

A comparison is much more intuitive than a comparison in the time-domain. For example, the standard elastic tunneling models predict a recovery of the form [26, 27]

\[
\Delta V_{th}(t_s, t_r) \approx A \log(1 + B t_s/t_r) \tag{2}
\]

with parameters \( A \) and \( B \). At a first glance, this appears compatible with experimental recovery data and similar models have been used frequently [28–30]. However, the CET map predicted by the elastic tunneling model, obtained from eq. (2)
2nm HfSiO
V$\text{th} = 2.7$V
T = 25$^\circ$C

![Graph 1](image1.png)

2nm HfSiON
V$\text{th} = 2.7$V
T = 125$^\circ$C

![Graph 2](image2.png)

**Fig. 2.** Two extreme cases of recovery after DC and AC stress for the non-nitrided HfSiO device at 25$^\circ$C (left) and the nitrided HfSiON device at 125$^\circ$C. As already demonstrated in [7, 22] for PBTI recovery after AC stress of duration $2 \times t_e$ merges with the DC recovery after stress of duration $t_e$ at $t_e = t_c$. The analytic model (solid lines for DC and dashed lines for AC) reproduces the data very well.

according to eq. (1), is

$$g(t_e, t_c) = \frac{AB}{(B + \frac{t_e}{t_c})^\gamma} \frac{t_e}{t_c} \quad \text{for} \quad t_e < t_{\text{max}}.$$  \hspace{1cm} (3)

which is a logistic distribution of the ratio $t_e/t_c$. The maximum emission time $t_{\text{max}}$ is on the order of seconds in thin (< 2nm) oxides. Furthermore, the correlation between $t_e$ and $t_c$ is much stronger than observed experimentally, see Fig. 1 (top), ruling this model out solely based on the CET map [23, 27] (not to mention the wrong bias and temperature dependence). Similar conclusions hold for the reaction-diffusion model [10], which even produces negative entries [27], see Fig. 1 (bottom).

Note, however, that the effective time constants in the CET map do not directly correspond to physical defect parameters like thermodynamic energy-levels or relaxation energies but are functions of them [27]. In this sense we wish to highlight that the CET map model is *not a new model meant to replace our previous modeling efforts* such as [24, 31]. Rather, the CET map model provides a convenient transformation of the experimental data to help understand the wide distribution of time constants. In particular, the CET map model can intuitively explain the effect of stress and recovery on a distributed set of defects, including low-frequency AC effects [21, 23].

In order to avoid technical issues with the second-order numerical derivative of experimental data and to facilitate our understanding of the distribution, we have recently suggested an analytic model for the CET map [23]. An additional benefit of this analytical model is that it allows for extrapolation out of the experimental window, allowing for an improved lifetime prediction. The analytic CET map uses a recoverable (R) and a permanent (P) component, both of which are represented by bivariate normal distributions for the effective activation energies of the correlated capture and emission times. Given recent experimental evidence [21, 24, 32–34], all time constants are assumed to be thermally activated, $\tau = \tau_c \exp \left( \frac{\beta E_A}{k_B T} \right)$, with $\beta = 1/k_B T_L$, $T_L$ the lattice temperature, and $k_B$ the Boltzmann constant. Based on the analytic CET map, the overall degradation can be *analytically* calculated. Compact expressions for digital switching between two discrete gate bias levels have been given for any combination of stress time/recovery time/duty factor, with excellent agreement to measurement data in the very wide window of stress and relaxation times from 1$\mu$s to 100ks [23]. While the accuracy of the model for DC and low-frequency AC stress is remarkable, see numerous comparisons in [23] and Fig. 2, discrepancies can be observed at higher frequencies, which will be the subject of the present paper.

**III. FREQUENCY DEPENDENCE**

Our discussion is based on the following simple prediction of the model for an AC stress with duty-factor $\alpha$ and thus on/off ratio $\gamma = \alpha/(1 - \alpha)$: Given that the duration of the AC stress equals $t_s/\alpha$, with the cumulative stress time $t_s$, the build-up of slowly recoverable traps with $t_e > t_s/\gamma$ is the same under both conditions [7], *independent of frequency*. The only difference is in the occupancy of the faster traps with $t_e < t_s/\gamma$. However, after a recovery time of $t_{\text{rec}} = t_s/\gamma$, these differences are wiped out, and AC and DC degradation must be the same. For example, with a duty-factor of 50%, we have $t_{\text{rec}} = t_s$. Then, recovery after a 2ks AC stress must match the recovery of a 1ks DC stress after $t_{\text{M}} = 1$ks. This is a simple consequence of the first-order reaction and completely independent of the actual distribution of the capture and emission times. Indeed, the merging of AC and DC recovery at the predicted recovery time has been experimentally confirmed for low-frequency AC PBTI on high-k [6, 7, 22] and low-frequency AC NBTI on...
SiO$_2$, SiON, HfSiO and HfSiON samples [23], see Fig. 2. An example demonstrating the occupancies of the defects in the CET map for a HfSiO device both directly after stress and at the merging point $t_M$ is given in Fig. 2. The occupancy times the defect density in the CET map is shown in Fig. 3: while the occupancy is significantly different right after stress (left panels), they are the same at $t_M$ (right panels).

One possible explanation for the controversial reports on the frequency dependence is that during AC stress the degradation oscillates between the cumulative stress and recovery levels. Any fast measurement result will therefore critically depend on the measurement delay which, ideally, should be synchronized with the on/off stress condition. However, according to the first-order model [7, 22], any remnants of this frequency-dependent component will have recovered after $t_R = t_M$. As such, in order to remove this uncertainty, we propose to check for a frequency dependent contribution to BTI with a deliberately large delay at the merging point $t_M$. This would also be favorable from the perspective of reaction-diffusion-based theories which claim that the frequency-dependent hole-trapping component vanishes after a few seconds, leaving behind the frequency-independent RD contribution [8, 35].

We have experimentally tested the validity of the above first-order model prediction on a number of technologies (SiO$_2$, SiON, HfSiO, and HfSiON) and consistently found that the predicted merging only occurs at low frequencies ($< 1\, \text{Hz} – 100\, \text{Hz}$). In Fig. 4 it is demonstrated how the degradation level decreases with increasing frequency. The discrepancy is about 10% for the SiON device but can reach levels of 30% in the HfSiO device measured, see Fig. 5. This effect cannot be reproduced by the first-order model no matter what parameters are used, since it is a direct consequence of the underlying first-order reaction. We conclude that either R or P (or both) cannot be described by a first-order reaction.

In order to attempt a separation of R and P, the AC stress is performed with different AC-off voltages, since it has been shown that R recovers much quicker under positive bias [24, 36–39]. Indeed, as shown in Fig. 6, particularly at an AC-off level of $+1\, \text{V}$, no frequency dependence is observed following the merging point $t_M$. We conclude that P can be described by a first-order model while R requires additional measures.

The CET map model is based on the assumption that the multi-state defect behavior observed previously [24] can be represented by an effective first-order (two-state) model. In particular, it was observed that the bias dependence of the effective capture time constant could be best explained by treating the change in the charge-state and the subsequent structural relaxation as a two-step process via an intermediate state 2’. The initial precursor state is given by 1 and the positively charged state is given by 2. Such a three-state model has also been used to explain the frequency dependence of PBTI in high-k pMOSFETs [16] under the assumption that the defects are negative-U centers. In addition it was observed that recovery may proceed via a metastable neutral state 1′. This pathway can dramatically reduce the emission time constant when the gate voltage goes below $V_{th}$ [40]. The full transition state diagram is shown below:

### IV. Advanced CET Map Model

Fig. 4. When at 50mHz the model (lines) agrees well with the data (symb), the model overestimates the degradation at higher frequencies, particularly in the non-nitried sample shown above.

![Fig. 4.](image1.png)

Fig. 5. Ratio of the AC (50%, 2ks) vs. DC(1ks) recovery at the theoretical merging point $t_M = 1ks$. At higher frequencies, the recovering AC degradation does no longer merge at $t_M$. Shown is data (symb) for a HfSiO device, where the effect is relatively strong, a HfSiON, and a SiON device. According to the first-order model, this ratio should be close to unity, which is obviously not the case.

![Fig. 5.](image2.png)

Fig. 6. When an AC stress is performed using the same on/off voltages as used during the subsequent recovery, the AC recovery after 2ks stress merges with the DC recovery after 1ks stress when $t_R = 1ks$, provided the frequency is low enough. When a more positive AC-off level is used instead of $V_o = -0.3\, \text{V}$, the frequency dependence gradually begins to disappear. This is strong evidence that R is frequency dependent but P is not [28].

![Fig. 6.](image3.png)
In order to get a first impression of the behavior of a two-step charging behavior, we will restrict our modeling attempts to the case $|V_G| > |V_{th}|$ and neglect the metastable neutral state 1'. As such, we obtain the following simplified defect model

\[
\begin{align*}
&\text{neutral} \\
&\text{positive} \\
1 & \xrightarrow{\tau_1} 2' \\
1 & \xrightarrow{e_1} 2 \\
2 & \xrightarrow{e_2} 2 \\
2' & \xrightarrow{\tau_2} 2
\end{align*}
\]

where the time constants $\tau_1$ and $\tau_2$ connect the metastable state with the neutral precursor state while $\tau_2$ and $\tau_3$ connect the metastable state with the positively charged state. Note that according to our previous model, only $\tau_1$ and $\tau_3$ depend on $V_G$, while $\tau_2$ and $\tau_3$ are thermal transitions over a barrier. Also, $\tau_1(V_{th})$ is very large and we neglect the contribution of state 2' to $\Delta V_{th}$.

Under DC conditions, the three-state defect can be approximated by a first-order two-state model using the effective capture and emission time constants [27]

\[
\begin{align*}
\tau_e &= \tau_1 + \tau_2 (1 + \tau_3/\tau_1), \\
\tau_c &= \tau_1 + \tau_2 (1 + \tau_3/\tau_2).
\end{align*}
\]

The approximation of a three-state defect by an effective two-state defect is valid provided the frequency does not become too large, in particular, $f < 1/\tau_1$.

For higher frequencies, the metastable state 2' acts like a low-pass filter. In order to further simplify the model, we only consider the forward rates during stress

\[
\begin{align*}
1 & \xrightarrow{e_1(V_s)} 2' \\
1 & \xrightarrow{e_1(V_s)} 2
\end{align*}
\]

and only the backward rates during recovery

\[
\begin{align*}
2 & \xrightarrow{e_2(V_r)} 2' \\
2 & \xrightarrow{e_2(V_r)} 2
\end{align*}
\]

where $V_s$ and $V_r$ are the gate voltages during stress and recovery, respectively. The low-pass effect is shown in Fig. 7: while the transition from state 1 to 2' shows the behavior of a two-state defect, that is, has a frequency dependence of the plateau value but not of the time constant, the transition from state 2' to 2 shows a frequency-dependent effective capture time.

As can be seen in that simple example, the effective capture time constant can show a marked frequency dependence in the three-state model. Such a frequency dependence is only obtained when $\tau_1 \gg \tau_3$ and $f < 1/\tau_1$, meaning that state 2' is completely emptied in every cycle. Otherwise, no frequency dependence is obtained. As such, for low enough frequencies, the three-state model simplifies to the two-state model. In particular, this implies that the predictions of the DC and low-frequency behavior are not affected by this extension of the model, provided the stress and relaxation times are larger than $\tau_1$ and $\tau_3$. As with the two-state model [7, 33], the response of the three-state defect to an AC signal can be evaluated in closed form, without the tedious requirement to resolve millions of cycles. While the derivation of the expressions is rather cumbersome compared to the elegant and simple solution of the two-state defect, they lead to a very simple results. In essence, under AC conditions, the capture time...
In particular, it is impossible to introduce a large difference in the experimental data while the three-state model can capture this effect. Using three-state defects for R, the duty-factor dependence can be accurately reproduced (lines). The factor \( w \) introduces a frequency dependence and is smaller than unity. Approximately, we have

\[
 w \approx \begin{cases} 
 1 & \text{for } f < f_c \\
 \alpha/2 \tau_1 f & \text{for } f_c < f < f_m \\
 \tau_1 \gamma/\tau_1 & \text{for } f_m < f 
\end{cases}
\]

with the corner frequency \( f_c = \alpha/2 \tau_1 \) and the maximum frequency \( f_m = (1 - \alpha)/2 \tau_1 \). Details of the derivation and additional consequences of the model will be published elsewhere. Using the above substitution, the analytical formulas given previously [23] remain valid, allowing for a very efficient analytic calculation of the AC degradation as a function of arbitrary stress and recovery times. Typical values used for \( \tau_1 \) are about 1ms and \( \tau_{2} \approx 0s \).

First, the model is evaluated on experimental data designed to reveal the merging point \( \Theta \) using 3 different duty-factors, see Fig. 8. As observed previously [7], the prediction of the two-state model is about 25% higher than the experimental data while the three-state model can capture this effect.

Second, although the two-state model can explain the qualitative features of the duty-factor dependence, comparison to experimental data remains unsatisfactory, see Fig. 9 (top). In particular, it is impossible to introduce a large difference between \( \alpha = 100\% \) (DC) and \( \alpha = 50\% \) (AC) without significantly impacting the model accuracy for DC stress. As such, the simulated step is never as pronounced as that observed experimentally. Much better agreement is obtained with the three-state model as shown in Fig. 9 (bottom) and Fig. 10. Remarkably, the ubiquitous shape of the curve is preserved even after a recovery time of 1ks, including the peak at\( \alpha = 100\% \). This is in stark contrast to RD theory papers [35], which claim that this peak is an artifact due to hole trapping and that the ‘real’ duty-factor dependence is given by RD theory. Quite to the contrary, given the preserved peak, we conclude again that hole trapping essentially determines NBTI even for longer stress and recovery times [8].

Third, the model is evaluated against the data recorded on the HiSiO device, which shows the strongest frequency dependence of 30% at 10kHz. Again, while the two-state model shows no frequency dependence after a sufficiently long recovery period, the three-state model is consistent with the experimental data as shown in Fig. 11. In particular, even after a long recovery period, AC and DC data do not merge.

Finally, we evaluate the bias dependence of the three-state CET map model to validate the assumptions derived from Fig. 6. For this, the parameters of the CET map need to be made bias-dependent. It has previously been shown that a considerable fraction of the BTI defects are switching traps, that is, contain at least three states [31]. These switching traps show an exponential dependence on the recovery bias below the threshold voltage [24]. Thus, to the first order, we capture the effect of the recovery voltage on the CET map by...
making the mean emission time of R bias-dependent. In fact, a simple linear relationship which changed the mean value of the effective activation energy by 300mV for a change by 1V in the gate bias proved to be sufficient. Figs. 12 and 13 shows the evaluation of this simple model against experimental data using 4 different AC-off voltages. Again, the three-state model captures the essence.

V. CONCLUSIONS

We have studied the frequency dependence of BTI by using our previously developed capture/emission time map model, which is based on first-order reactions. While previous studies on the frequency dependence published in literature probably suffered from various issues – such as unspecified delay and a mixture of AC and recovery effects in the measured degradation level – our study deliberately uses long recovery times equal to the theoretical first-order AC/DC merging point. The observed deviation from the first-order model means that defect charging follows first-order kinetics only in the low-frequency limit. Consistent with the previously described switching traps, introduction of a third defect state provides a good description of the experimentally observed frequency dependence for a number of different technologies.

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