

## Recent advances in the spherical harmonics expansion of the Boltzmann transport equation

*Karl Rupp*

Institute for Analysis and Scientific Computing, TU Wien  
Wiedner Hauptstraße 8-10/E101, A-1040 Wien, Austria

`rupp@iue.tuwien.ac.at`

*Tibor Grasser*

Institute for Microelectronics, TU Wien  
Gußhausstraße 27-29/E360, A-1040 Wien, Austria

`grasser@iue.tuwien.ac.at`

*Ansgar Jüngel*

Institute for Analysis and Scientific Computing, TU Wien  
Wiedner Hauptstraße 8-10/E101, A-1040 Wien, Austria

`juengel@asc.tuwien.ac.at`

Since typically employed macroscopic transport models are invalid in the deca-nanometer regime, accurate semiclassical simulation of carrier transport in semiconductors requires the solution of Boltzmann's transport equation. To overcome the deficiencies of stochastic Monte Carlo techniques, a deterministic solution approach based on a spherical harmonics expansion (SHE) has become increasingly attractive over the last years [1]. Unfortunately, the high computational effort of the SHE method has so far prevented its application to 3D geometries. We refine the SHE method by suggesting and evaluating adaptive variable-order expansions, a system matrix compression scheme for keeping the memory consumption at high expansion orders moderate, a parallel preconditioner for accelerating the solution of the resulting system of linear equations, and demonstrate an efficient implementation of the proposed algorithms on unstructured grids. The combination of these techniques allows for the efficient solution of higher-order expansions not only in low-dimensional devices, but also in the uncharted 3D regime.

1. Hong, S. M. and Jungemann C. 2011 *Deterministic Solvers for the Boltzmann Transport Equation*. Springer.