## **Spin-dependent Resonant Tunneling** in Ferromagnet-Oxide-Silicon Structures

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## 1. Introduction

Silicon, the main material of microelectronics, is perfectly suited for spin-driven applications due to its weak spin-orbit interaction and long spin lifetime [1,2]. Spin injection from a ferromagnetic electrode into *n*-silicon was claimed at room temperature [3] and also at elevated temperatures [4]. However, the amplitude of the signal extracted from a three-terminal injection method [3,4] is orders of magnitude larger than that predicted by a theory [1], provided the signal is caused by spin accumulation in silicon. Possible reasons for this discrepancy are currently heavily debated [1,5-8]. An alternative interpretation of the three-terminal signal magnitude based on spin-dependent magnetoresistance due to trap-assisted resonant tunneling was proposed [5]; however, the effects of spin dynamics and spin relaxation [6], which are important at room temperature, were not taken properly into consideration. Our goal has been to investigate the role of the spin dynamics on a trap including spin relaxation and decoherence in order to determine the trap-assisted tunneling magnetoresistance.

## 2. Method and Results

To highlight the role of spin relaxation and decoherence we introduce the corresponding relaxation terms into a Lindblad equation for the density matrix evolution of spin on a trap.

$$\rho = \alpha I + a\sigma_x' + b\sigma_y' + c\sigma_z' \tag{1}$$

Here a,b,c are the spin projection expectation values on the axes x',y',z', with the z' axis along the direction of the local magnetic field on the trap. The tunneling rate  $\Gamma_{\rm N}$  from silicon to a trap does not depend on spin, while the tunneling rate  $\Gamma_{\pm} = \Gamma_{\rm F}(1\pm p)$  from the trap to a ferromagnet depends on the spin projection  $\sigma=\pm$  on the magnetization direction; here  $p{\le}1$  is the interfacial current polarization in the ferromagnet. Assuming the local magnetic field on the trap is tilted by an angle  $\Theta$  with respect to the magnetization (Fig.1), the following system of coupled stationary equations for the density matrix coefficients is obtained:

$$b\omega_L + c\left(\frac{1}{T_2} + \Gamma_F\right) = 0 \tag{2}$$

$$c \,\omega_L \cos(\Theta) - a \sin(\Theta) \left(\frac{1}{T_1} + \Gamma_F\right) \\ - b \cos(\Theta) \left(\frac{1}{T_2} + \Gamma_F\right) = 0 \tag{3}$$

$$b \sin(\Theta) \left( \frac{1}{T_2} + \Gamma_F \right) - a \cos(\Theta) \left( \frac{1}{T_1} + \Gamma_F \right) - c \omega_L \sin(\Theta) = p \Gamma_F \alpha$$
 (4)

$$(\Gamma_F + \Gamma_N)\alpha + p\Gamma_F(a\cos(\Theta) - b\sin(\Theta)) = \Gamma_N \quad (5)$$

Here  $\omega_L$  is the spin precession Larmor frequency. The master equations include the spin lifetime  $T_1$  and coherence time  $T_2$  (typically  $T_2 \le T_1$ ). The current I due to tunneling via a trap is computed as

$$I = e \, \hat{\Gamma}_F (1 - \alpha). \tag{6}$$

The current I differs from  $I_0 = \Gamma_F \Gamma_N / (\Gamma_F + \Gamma_N)$  and depends on the angle  $\Theta$  between the spin quantization axis and the magnetization orientation. Solving equations (2-6) results in the following expressions:

$$I = e \frac{\Gamma_F(\Theta) \Gamma_N}{\Gamma_F(\Theta) + \Gamma_N}$$

$$\Gamma_F(\Theta) = \Gamma_F \left( 1 - p^2 \Gamma_F T_1 \left\{ \frac{\cos^2 \Theta}{\Gamma_F T_1 + 1} + \frac{T_2}{T_1} \frac{\sin^2 \Theta (\Gamma_F T_2 + 1)}{\omega_L^2 T_2^2 + (\Gamma_F T_2 + 1)^2} \right\} \right) (6)$$

In the case  $T_1 = T_2 \rightarrow \infty$  one obtains

$$\Gamma_F(\Theta) = \Gamma_F \left( 1 - p^2 \left\{ \cos^2 \Theta + \frac{\sin^2 \Theta}{\omega_L^2 / \Gamma_F^2 + 1} \right\} \right),$$

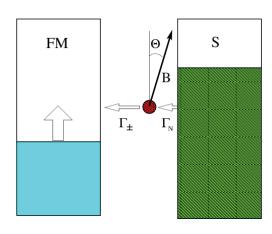
which is the corresponding expression for *I* from [5]

In extension to [5], (7) includes the effects of spin relaxation. When  $\Gamma_F T_1 = \Gamma_F T_2 \ll 1$ , the resistance dependence on the magnetic field is a Lorentzian function with the half-width determined by the inverse spin lifetime. A short spin relaxation time suppresses the "spin blockade" [5], which appeared at small  $\Theta$ (Fig.2), in a similar fashion as the reduction of spin current polarization p (Fig.3). Due to the suppression of the last term in (6) at short  $T_2$  with  $T_1$  fixed, the amplitude of the  $I(\Theta)$  modulation with  $\Theta$  becomes more pronounced (Fig.4), in contrast to the intuitive expectation that strong decoherence should reduce the effect. In contrast to [5], at finite  $T_1$  the modulation of  $I(\Theta)$  is present at an arbitrary trap position relative to the contacts (Fig.5). Finally, an unusual non-monotonic dependence with  $T_2$  of the magnetoresistance half-width as a function of the perpendicular magnetic field B, with the linewidth decreasing, at shorter  $T_2$  is shown in Fig.6.

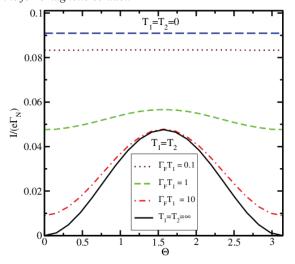
## References

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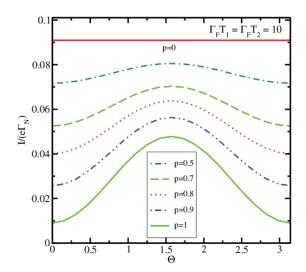
This work is supported by the ERC grant #247056 MOSILSPIN.



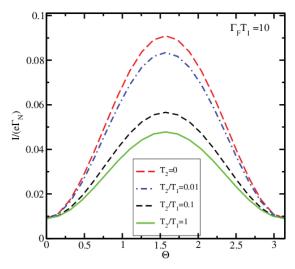
**Fig.1:** An electron tunnels with the rate  $\Gamma_N$  on the trap and  $\Gamma_\pm$  to the ferromagnet. A magnetic field **B** defines the trap spin quantization axis OZ', which is at an angle  $\Theta$  to the magnetization orientation OZ in the ferromagnetic contact.



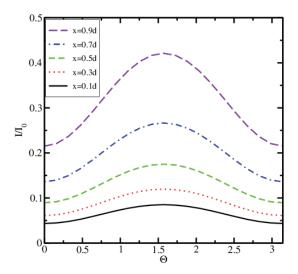
**Fig.2:** Current in units of  $e\Gamma_N$  as a function of  $\Theta$  for p=1  $\Gamma_N/\Gamma_F=10$ ,  $\omega_L/\Gamma_F=1$ , and several values of  $T_2=T_L$ .



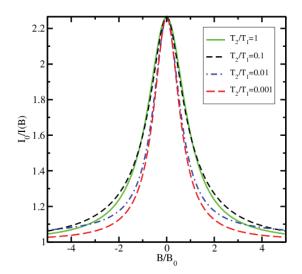
**Fig.3:** Current as a function of  $\Theta$ , for  $\Gamma_N/\Gamma_F = 10$ ,  $\omega_L/\Gamma_F = 1$ ,  $\Gamma_F T_I = \Gamma_F T_I = 10$ , and several values of p.



**Fig.4:** Current as a function of  $\Theta$ , for p=1,  $\Gamma_N/\Gamma_F=10$ ,  $\omega_L/\Gamma_F=1$ ,  $\Gamma_F T_I=10$ , and several values of  $T_2/T_I$ .



**Fig.5:** Normalized current as a function of the position x, for p=1,  $\Gamma_N = \Gamma_0 \exp(-x/d)$ ,  $\Gamma_F = \Gamma_0 \exp(-(d-x)/d)$ ,  $T_2 = T_1$ ,  $\omega_L T_2 = \Gamma_0 T_2 = 10$ 



**Fig.6:** Magnetoresistance signal as a function of the perpendicular magnetic field **B** for several  $T_2/T_1$ , for p=0.8 and  $\Gamma_F T_1=10$ . The field **B**<sub>0</sub> is parallel to the magnetization in the ferromagnet.