

## NOTE

### SIMPLE AND ACCURATE REPRESENTATION OF IMPLANTATION PARAMETERS BY LOW ORDER POLYNOMIALS

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#### INTRODUCTION

Ion implantation is an indispensable step in the process of producing modern integrated circuits. Thereby, in particular in silicon technology, the elements B, P, As and Sb are implanted. By the implantation process gaussian profiles are generated[1-4]. In practice such profiles are characterized by the projected range ( $R_p$ ) and the projected standard deviation ( $\Delta R_p$ ). These parameters are fairly complicated functions of the implantation energy ( $E$ ), the element, the substrate and other physical parameters. For the practical performance of ion implantation the values  $R_p$  and  $\Delta R_p$ , being dependent on energy are listed in tables for various materials and elements. The values are deduced from theory as well as from experiments[3, 5].

A considerable disadvantage of such tables is that they are unhandy. Furthermore, one has to interpolate between values. Introducing such tables in numerical implantation programs precious memory space is wasted. Moreover the interpolation requires additional calculations.

This note intends to find simple functions of  $R_p$  and  $\Delta R_p$  in dependence of the implantation energy in order to eliminate the above mentioned disadvantages.

The values of  $R_p$  and  $\Delta R_p$  of B, As, P and Sb in Si, SiO<sub>2</sub> and Si<sub>3</sub>N<sub>4</sub> are approximated by the following polynomials

$$R_p = \sum_{i=1}^{N_1} (A1)_i E^i$$

$$\Delta R_p = \sum_{i=1}^{N_2} (A2)_i E^i$$

Tables 1-3 give the coefficients of the polynomials for various elements and substrates.

From the practical point of view the representation of  $R_p$  and  $\Delta R_p$  by the above polynomials is more accurate and simpler than by tables.

The accuracy  $R_p$  and  $\Delta R_p$  if calculated by polynomials is better than 10% in an energy range between 10 and 300 keV. These polynomials may also be inserted in computer programs with minimal expense, and intermediate values may be gained directly without interpolation.

Table 1. Coefficient (A1)<sub>i</sub> and (A2)<sub>i</sub> of the polynomials for the elements As, B, P and Sb in silicon

i	As/Si		B/Si	
	(A1) <sub>i</sub>	(A2) <sub>i</sub>	(A1) <sub>i</sub>	(A2) <sub>i</sub>
1	9.818E-4	3.652E-4	3.338E-3	1.781E-3
2	-1.022E-5	-3.820E-6	-3.308E-6	-2.086E-5
3	9.067E-8	3.235E-8		1.403E-7
4	-3.422E-10	-1.202E-10		-4.545E-10
5	4.608E-13	1.601E-13		5.525E-13

i	P/Si		Sb/Si	
	(A1) <sub>i</sub>	(A2) <sub>i</sub>	(A1) <sub>i</sub>	(A2) <sub>i</sub>
1	1.259E-3	6.542E-4	8.887E-4	2.674E-4
2	-2.743E-7	-3.161E-6	-1.013E-5	-2.885E-6
3	1.290E-9	1.371E-8	8.372E-8	2.311E-8
4		-2.252E-11	-3.056E-10	-8.310E-11
5			4.028E-13	1.084E-13

Table 2. Coefficients (A1)<sub>i</sub> and (A2)<sub>i</sub> of the polynomials for the elements As, B, P and Sb in SiO<sub>2</sub>

i	<u>As/SiO<sub>2</sub></u>		<u>B/SiO<sub>2</sub></u>	
	(A1) <sub>i</sub>	(A2) <sub>i</sub>	(A1) <sub>i</sub>	(A2) <sub>i</sub>
1	7.806E-4	2.637E-4	3.258E-3	1.433E-3
2	-7.899E-6	-2.762E-6	-2.113E-6	-1.077E-5
3	7.029E-8	2.373E-8		4.190E-8
4	-2.653E-10	-8.899E-11		-6.000E-11
5	3.573E-13	1.193E-13		

i	<u>P/SiO<sub>2</sub></u>		<u>Sb/SiO<sub>2</sub></u>	
	(A1) <sub>i</sub>	(A2) <sub>i</sub>	(A1) <sub>i</sub>	(A2) <sub>i</sub>
1	9.842E-4	4.591E-4	7.200E-4	2.018E-4
2	2.240E-7	-1.983E-6	-8.054E-6	-2.328E-6
3		8.383E-9	6.641E-8	1.917E-8
4		-1.382E-11	-2.422E-10	-6.997E-11
5			3.191E-13	9.211E-14

Table 3. Coefficients (A1)<sub>i</sub> and (A2)<sub>i</sub> of the polynomials for the elements As, B, P and Sb in Si<sub>3</sub>N<sub>4</sub>

i	<u>As/Si<sub>3</sub>N<sub>4</sub></u>		<u>B/Si<sub>3</sub>N<sub>4</sub></u>	
	(A1) <sub>i</sub>	(A2) <sub>i</sub>	(A1) <sub>i</sub>	(A2) <sub>i</sub>
1	6.094E-4	2.035E-4	2.514E-3	1.115E-3
2	-6.213E-6	-2.092E-6	-1.618E-6	-8.328E-6
3	5.516E-8	1.787E-8		3.228E-8
4	-2.080E-10	-6.678E-11		-4.612E-11
5	2.799E-13	8.932E-14		

i	<u>P/Si<sub>3</sub>N<sub>4</sub></u>		<u>Sb/Si<sub>3</sub>N<sub>4</sub></u>	
	(A1) <sub>i</sub>	(A2) <sub>i</sub>	(A1) <sub>i</sub>	(A2) <sub>i</sub>
1	7.617E-4	3.542E-4	5.660E-4	1.516E-4
2	1.681E-7	-1.488E-6	-6.440E-6	-1.655E-6
3		6.204E-9	5.323E-8	1.345E-8
4		-1.019E-11	-1.944E-10	-4.878E-11
5			2.563E-13	6.401E-14

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